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The Point of Concern about the Implementation of Liability-Driven Investment (LDI) in a Pension Plan in Japan

ARIHIRO OKAMOTO

The Sumitomo Trust & Banking Co., Ltd.

Pension Consulting Department

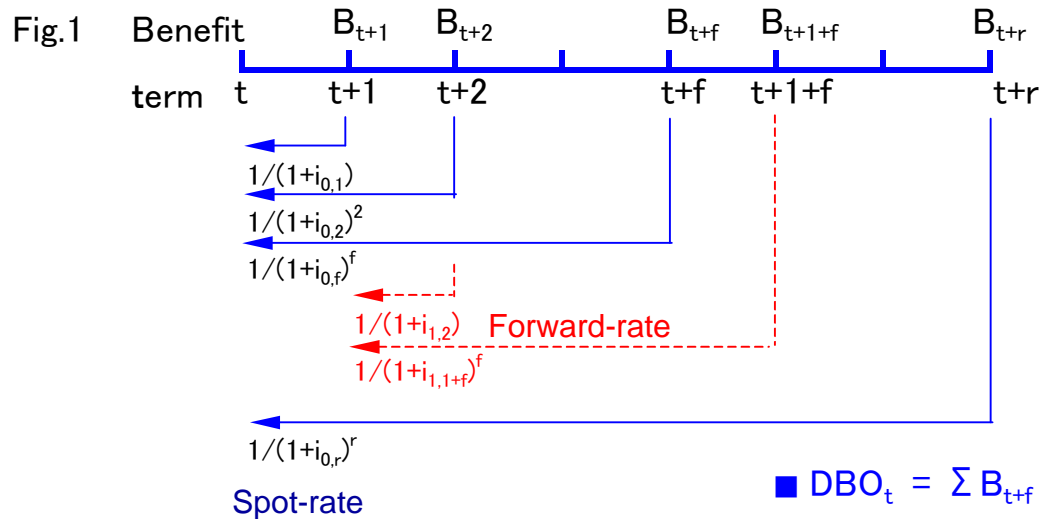


1. Introduction

- The immediate recognition is examined on IFRSs
- LDI would become one of the attractive alternatives of the pension investment strategy
- LDI looks uncommon in Japan, although LDI in frozen pension plans in UK and US are reported
 - Few frozen pension plans
 - The period of the liability is too long to set the bonds
 - The current interest rate is too low and the further bond investment does not look like a wise strategy
- The future accruals might complicate LDI in an active pension plan.
- I discuss the asset allocation method which allows an active pension plan to carry out LDI

2~4. DBO (Defined Benefit Obligation)

2. DBO and a net cash-flow



$$\blacksquare \text{ DBO}_t = \sum B_{t+f} \frac{t}{t+f} \frac{1}{(1+i_{0,f})^f} \quad \dots (\text{eq-1})$$

$$\text{DBO}_t = B_{t+1} \frac{t}{t+1} \frac{1}{1+i_{0,1}} + B_{t+2} \frac{t}{t+2} \frac{1}{(1+i_{0,2})^2} + \dots$$

$$\text{DBO}_{t+1} = B_{t+1+1} \frac{t+1}{t+1+1} \frac{1}{1+i_{1,2}} + B_{t+1+2} \frac{t+1}{t+1+2} \frac{1}{(1+i_{1,3})^2} + \dots$$

$$= \text{DBO}_t (1+i_{0,1}) + \text{DBO}_t \frac{1+i_{0,1}}{t} - B_{t+1}$$

$$= \text{DBO}_t (1+i_{0,1}) + \text{SC}_{t+1} - B_{t+1}$$

$$= \text{DBO}_t (1+i_{0,1}) - \text{CF}_{t+1}$$

$$\text{DBO}_t = \text{CF}_{t+1}/(1+i_{0,1}) + \text{DBO}_{t+1}/(1+i_{0,1})$$

Net cash-flow

$$\blacksquare \text{ CF}_{t+1} = B_{t+1} - \text{SC}_{t+1} \quad \dots (\text{eq-2})$$

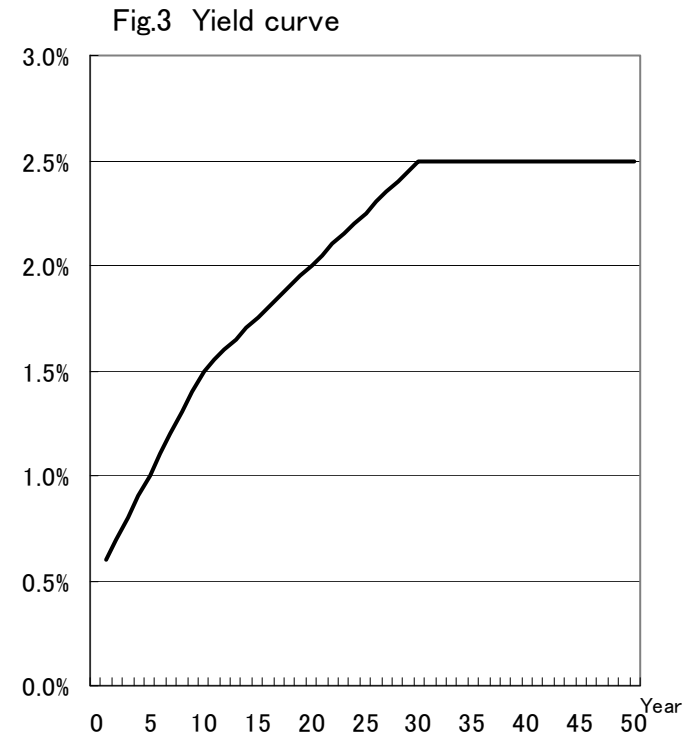
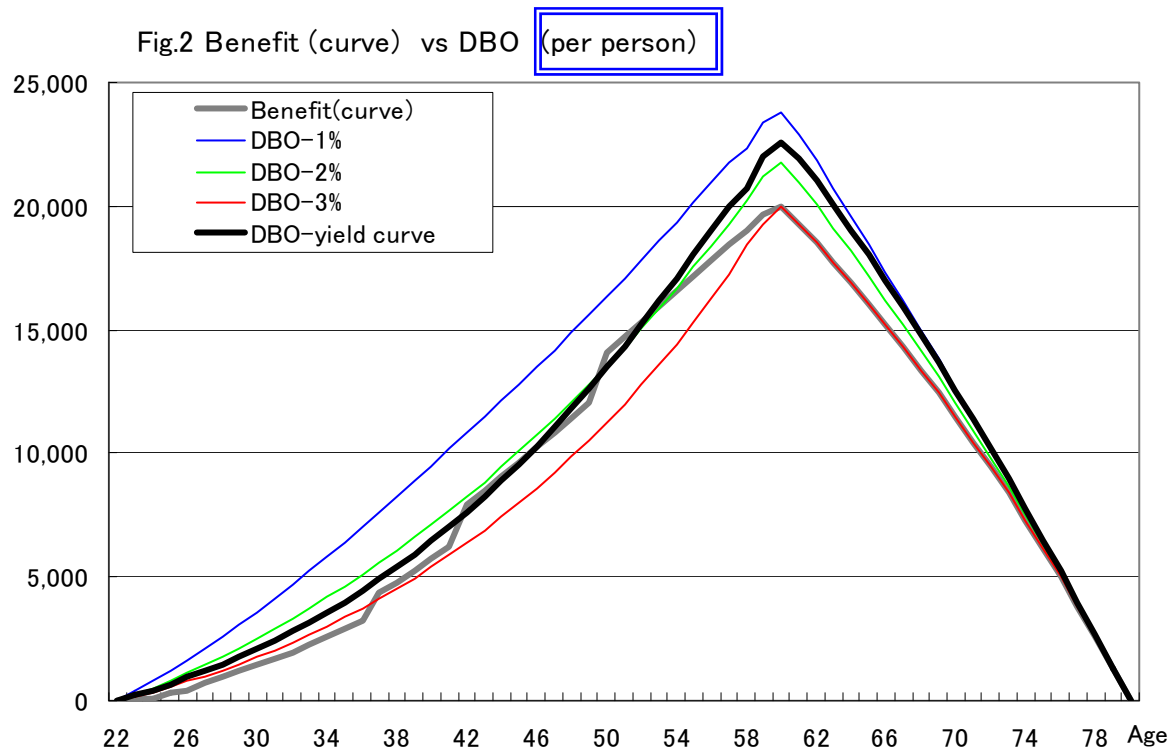
$$\blacksquare \text{ DBO}_t = \sum \text{CF}_{t+f}/(1+i_{0,f})^f \quad \dots (\text{eq-3})$$

$$\text{SC}_{t+1} = \text{DBO}_t \frac{1+i_{0,1}}{t} = \sum B_{t+f} \frac{1}{t+f} \frac{1+i_{0,1}}{(1+i_{0,f})^f}$$

Calculated by forward-rate

$$\blacksquare \text{ SC}_{t+2} = \text{DBO}_{t+1} \frac{1+i_{1,2}}{t+1} = \sum B_{t+1+f} \frac{1}{t+1+f} \frac{1+i_{1,2}}{(1+i_{1,1+f})^f} \quad \dots (\text{eq-4})$$

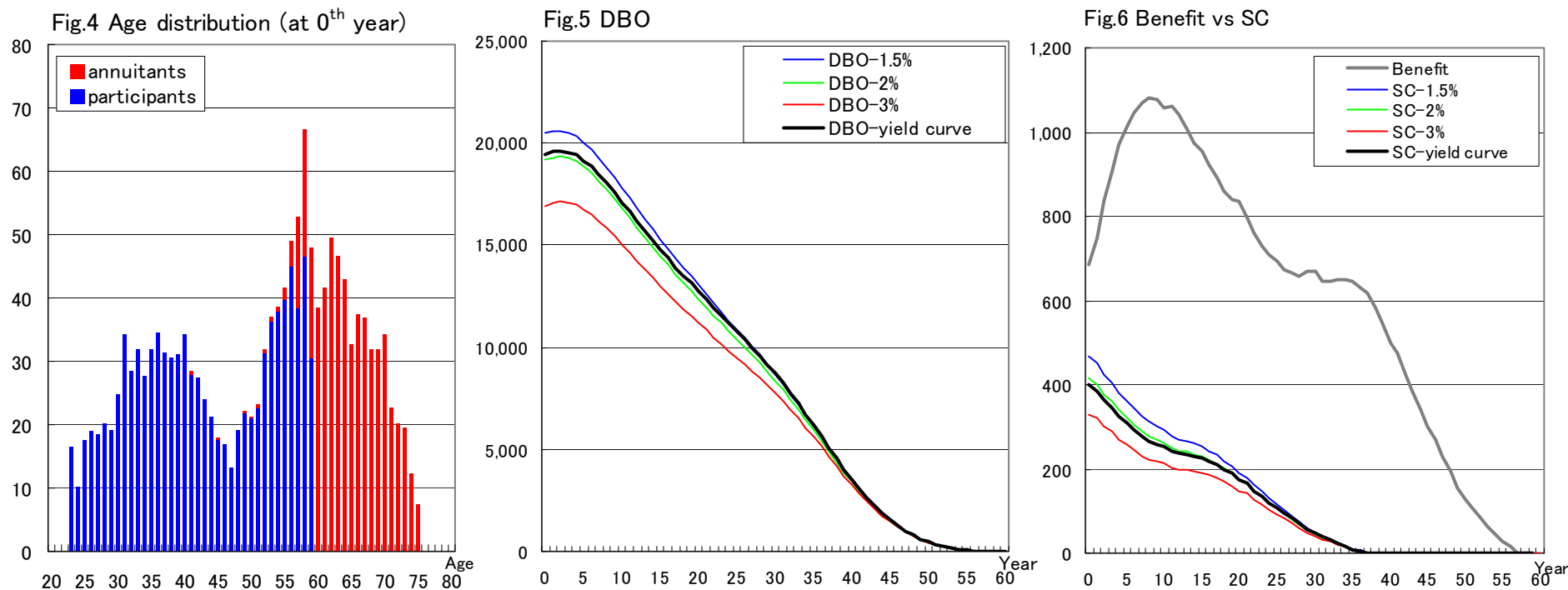
3. The characteristic of DBO by the examples



■ DBO(by yield curve) \doteq DBO(by 2%)

- Join the plan at age 22
- The pension benefit starts from at age 60 and lasts for 20 years
- Interest rate during annuitant is 3.0%

4. DBO with the pension plan



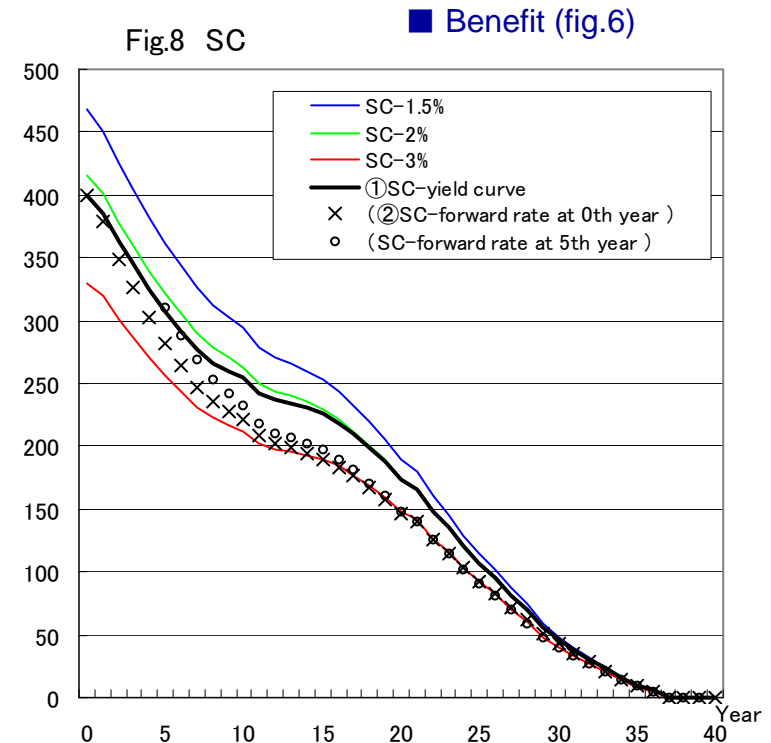
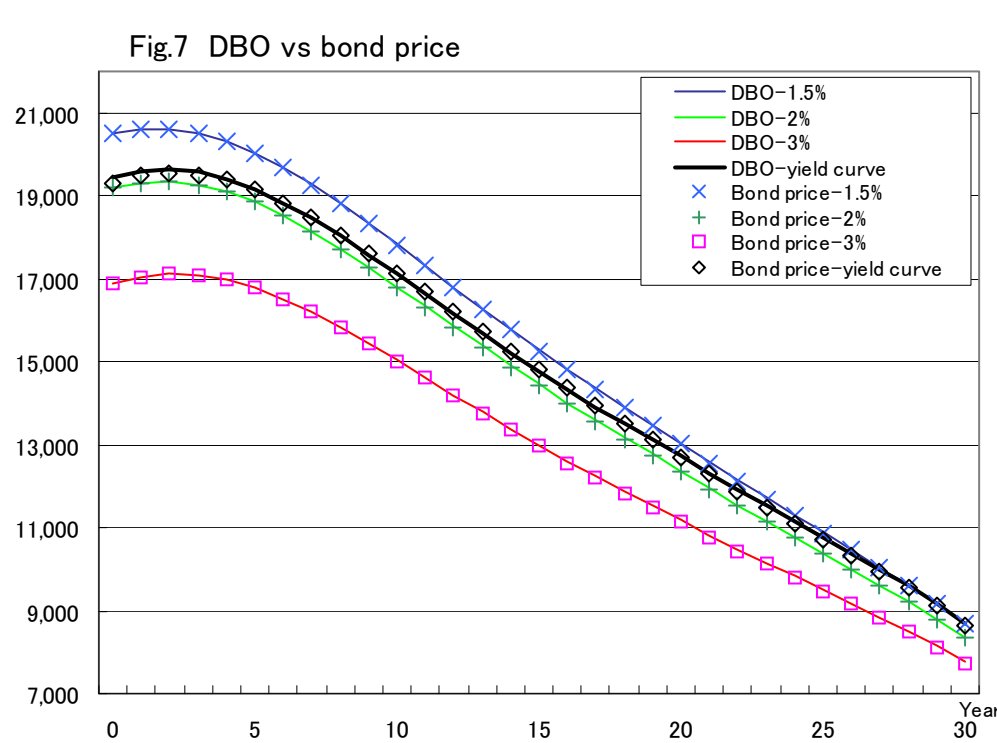
■ DBO(by yield curve) \doteq DBO(by 2%)

■ SC(by yield curve) \doteq SC(by 2%)

- No participant joins
- Lump sum choice rate 0%
- The yield curve(fig.3) is used for each year (no change of interest rates)

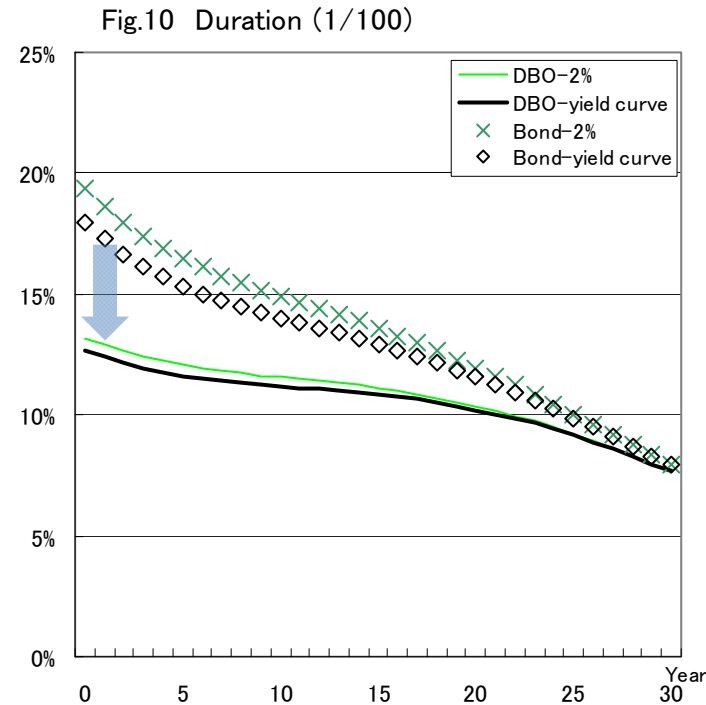
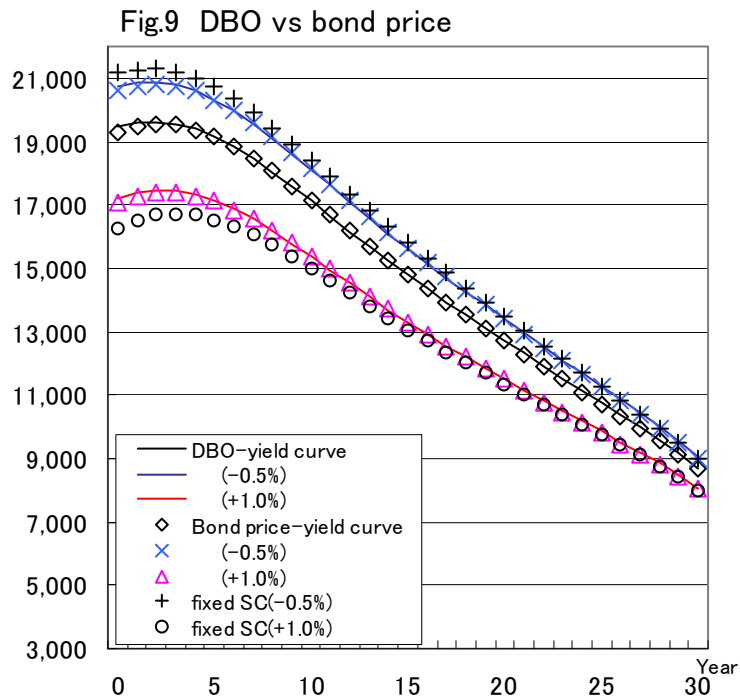
5. LDI by the bond

5-1 The net cash-flow matching



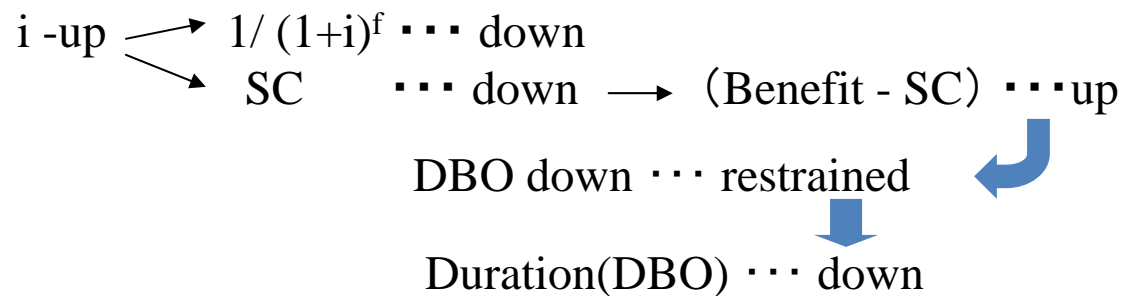
- DBO = The bond price (making the portfolio which corresponds to the net cash-flow (benefit - SC) of each year)
- DBO(by yield curve) is calculated by SC based on a forward-rate
 - The yield curve(fig.3) is used for each year (no change of interest rates)
 - Contributions of the same amount of SC are injected
 - The bond is interest-bearing securities (government bond)

5-2 The duration



■ Duration(DBO) < Duration(Bond)

■ $DBO = \sum (Benefit - SC) / (1+i)^f$



5-3 Bond portfolio for the duration matching

- The net cash-flow matching \neq The duration matching ($\text{Duration}(\text{DBO}) < \text{Duration}(\text{Bond})$)
- Two merits to make the duration of the bond smaller
 - (1) to make a bond portfolio without using the super long-term bond (beyond 30 years)
 - (2) to increase short-term bonds, to make the portfolio to be prepared for a lot of payments by the lump sum choice
- Bond portfolio
 - (1) Using the interest-bearing securities of a term equal to or less than 30 years
 - (2) Increasing the short-term bonds to have payment even if the lump sum choice rate becomes 50% for five years
 - (3) Making the duration of the bond approximately corresponds to the duration of DBO without re-balancing for a period as long as possible

In addition, to reinvest the cash which remains by a coupon and a redemption with 30 years bonds
- I should have a lot of long-term bonds, when I increase short-term bonds to reduce the duration (so-called barbell-shaped)

5-4 LDI (lump sum choice rate 0%, no re-balance)

Fig.11 DBO vs bond price (lump sum choice rate 0%)

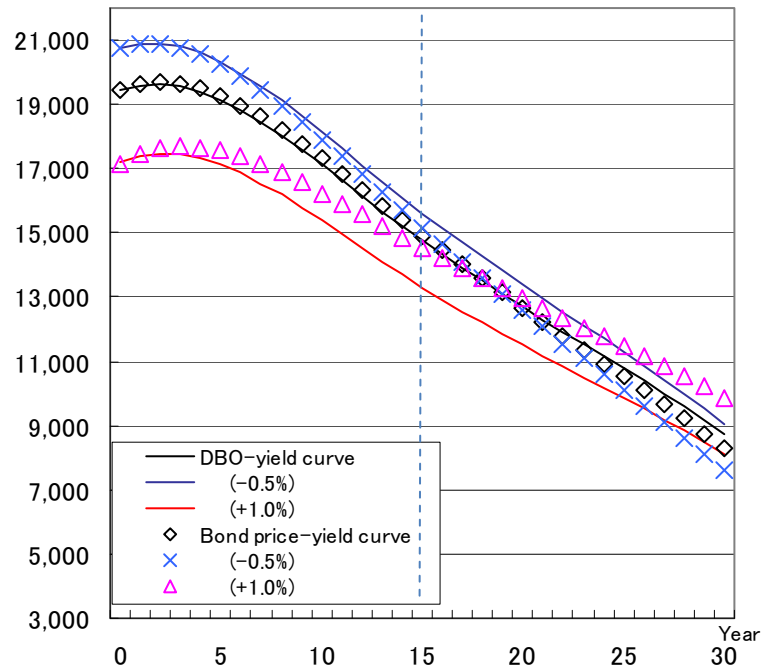
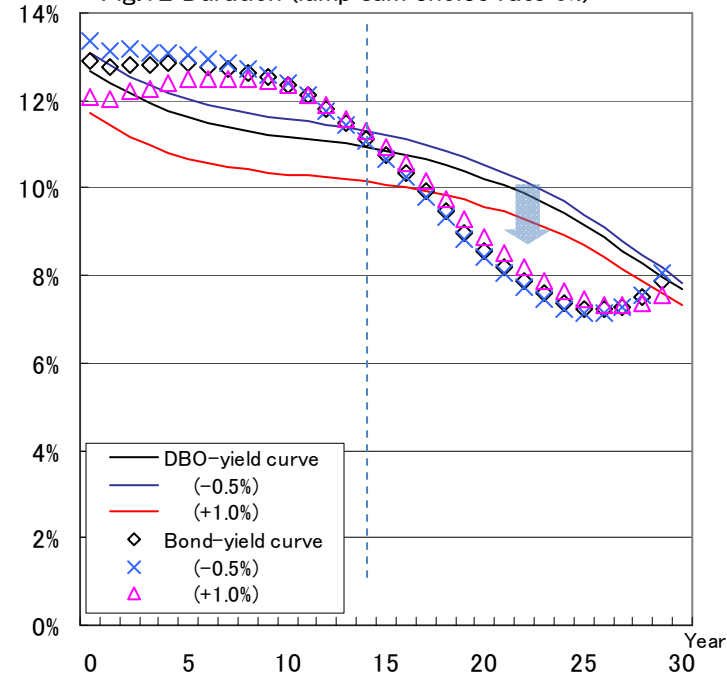


Fig.12 Duration (lump sum choice rate 0%)



■ $[t \leq 15 \text{ years}]$ DBO \doteq Bond price (no change of interest rates)

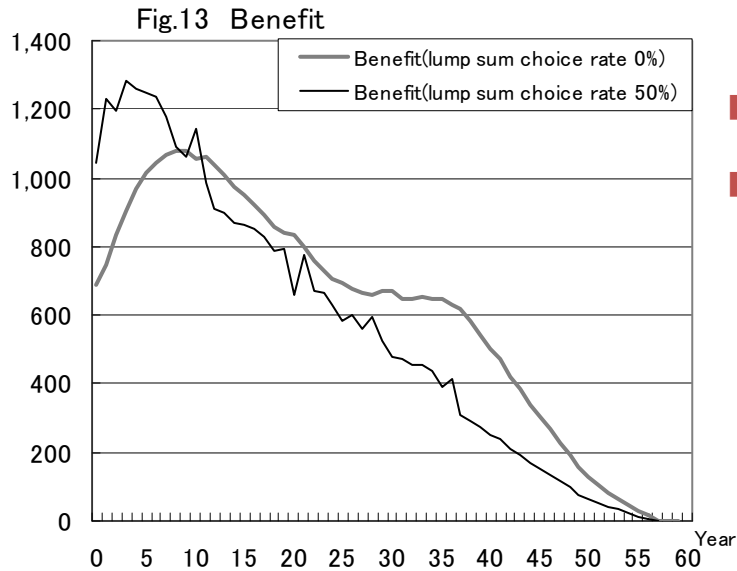
■ $[t > 15 \text{ years}]$ DBO $>$ Bond price (no change of interest rates)

↪ Duration(DBO) $>$ Duration(Bond)

■ [The interest rate rises] DBO $<$ Bond price

↪ $SC(\text{DBO}) < SC(\text{Bond}) (= SC(\text{no change of interest rates}))$

5-5 LDI (lump sum choice rate 50%, no re-balance)



- [No change of interest rate] $DBO < \text{Bond price}$
- [The interest rate falls] $DBO \doteq \text{Bond price}$
- The surplus by the lump sum choice (interest rate during annuitant 3%)

Fig.14 DBO vs bond price (lump sum choice rate 50%)

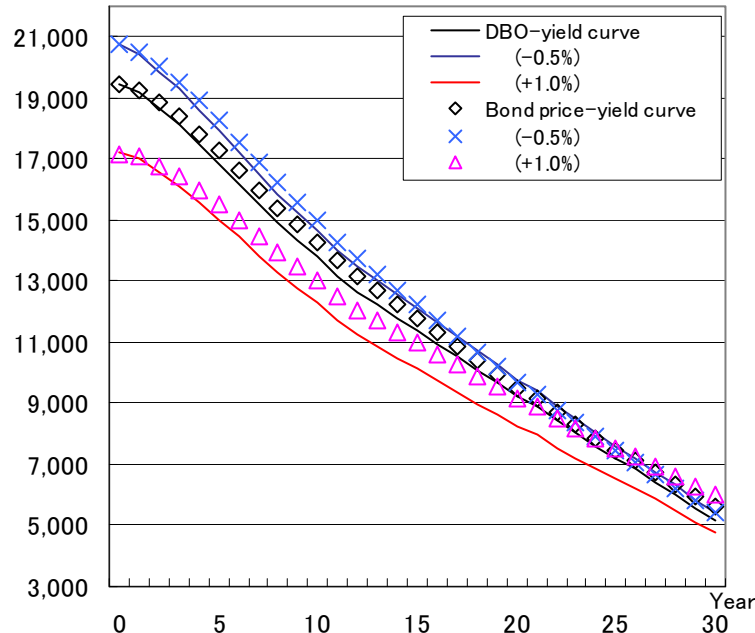
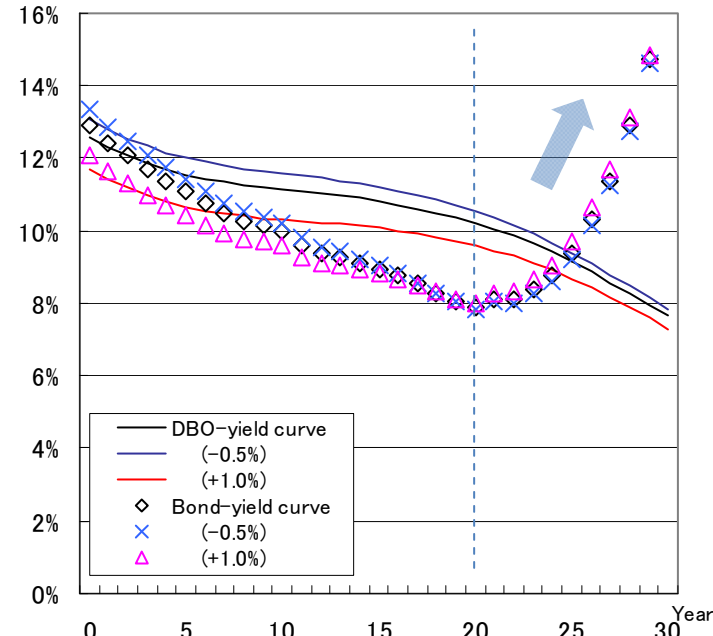


Fig.15 Duration (lump sum choice rate 50%)



5-6 LDI (if re-balance)

Fig.16 DBO vs bond price(lump sum choice rate 0%) re-balance

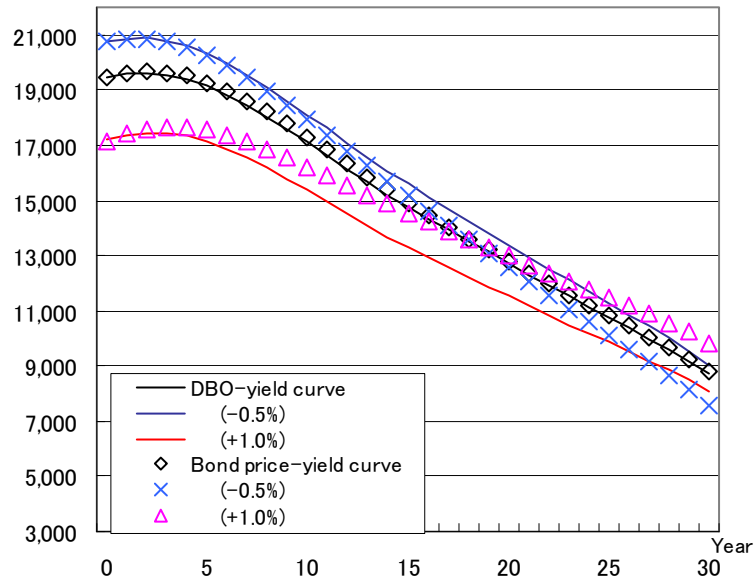


Fig.17 Duration(lump sum choice rate 0%) re-balance

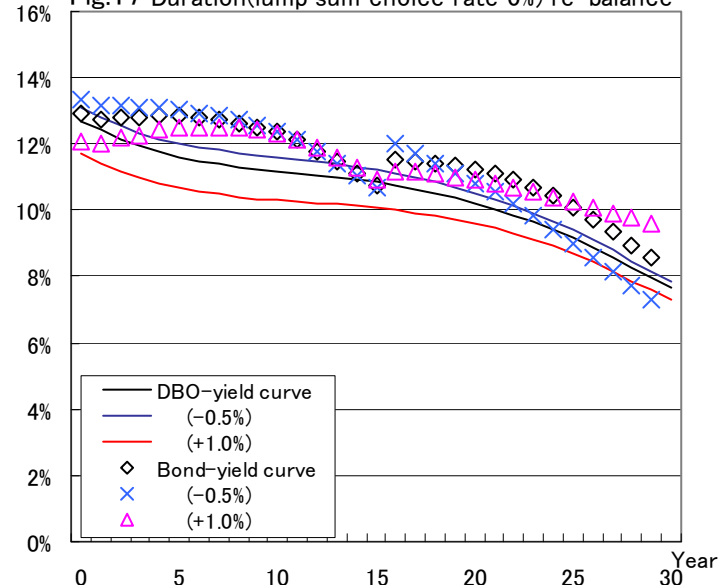


Fig.18 DBO vs bond price(lump sum choice rate 50%) re-balance

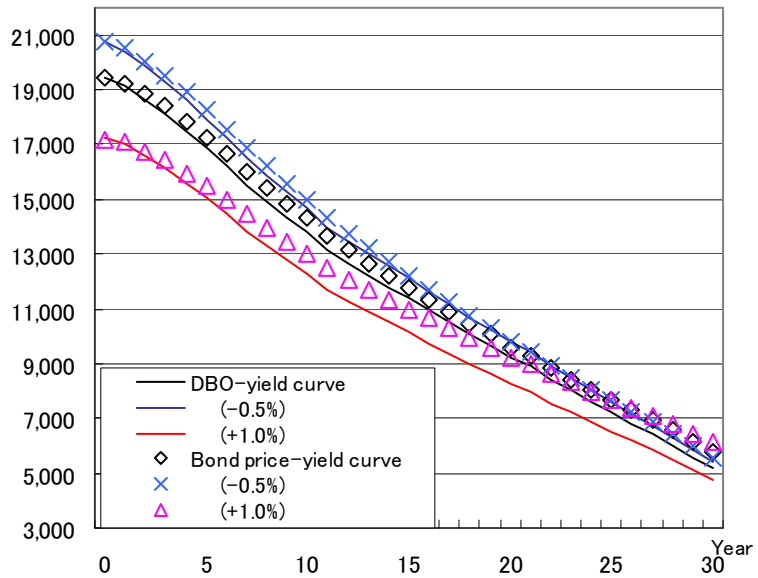
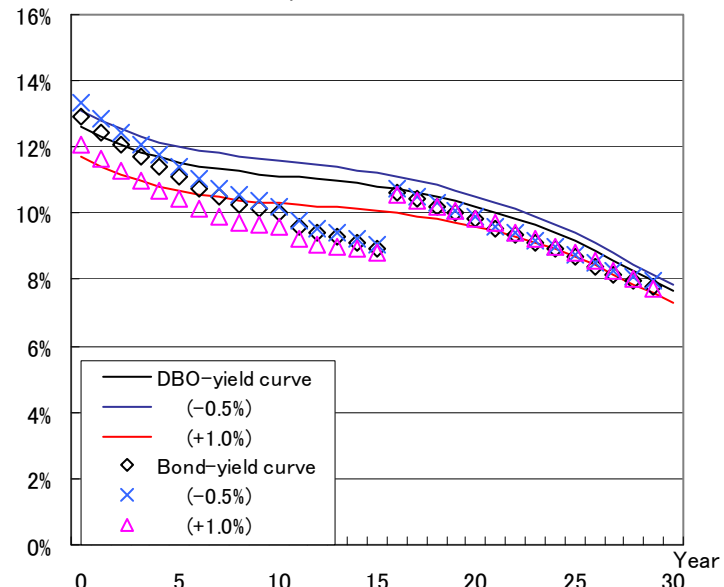
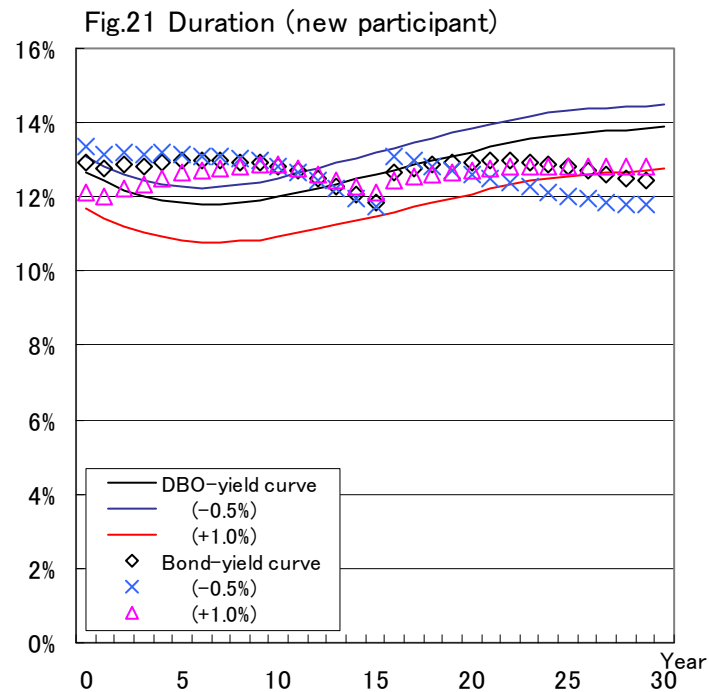
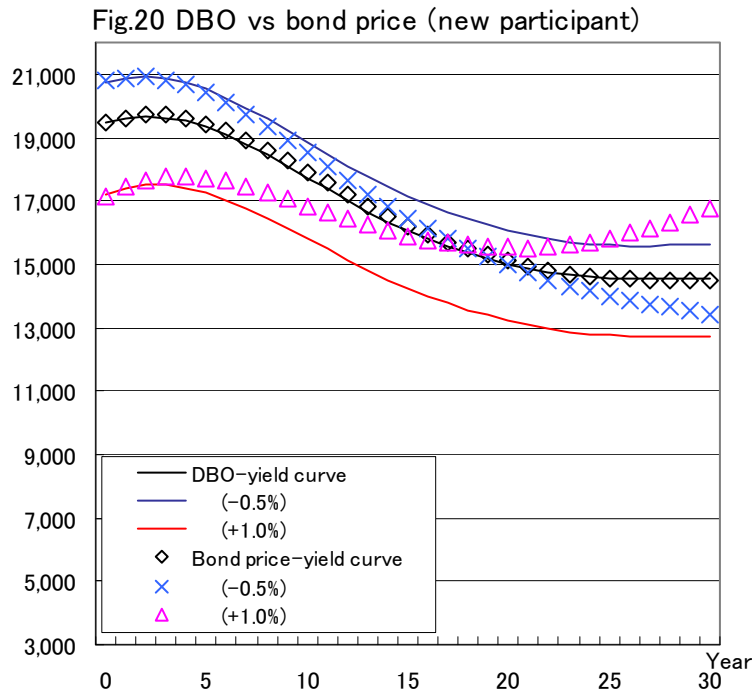


Fig.19 Duration(lump sum choice rate 50%) re-balance



5-7 LDI (new participant)



- The surplus hardly has a difference in case of no new participant(fig.16)
[no change of interest rates]
- Duration(new participant) > Duration(no new participant) ··· across the ages

- Join the plan at age 22
- Invest SC(contribution) in 30 years bonds

6. Summary

- The present value of the net cash-flow (Benefit – SC) = the amount of DBO
[in the active pension plan]
- It is possible theoretically to make a bond portfolio by this net cash-flow
- Net cash-flow matching \neq Duration matching
 - Duration(DBO) < Duration(Bond) ← SC changes by the change of interest rate
- It is possible to make a practical bond portfolio which the duration follows DBO under a certain condition
- I aimed to make the bond portfolio (1) in correspondence with changed payment and (2) which evaded re-balance as much as possible to hold down a cost
- Though I had thought that LDI in the active pension plan was difficult, I confirm that it is possible enough for business by the bond investment.
- However, full-scale LDI by the bond investment seems not to be carried out often by the reasons as follows in Japan currently
 - Few for DBO in full funding
 - The current interest rate is too low and the further bond investment does not look like a wise strategy
- When the consciousness of the company would be changed by “immediate recognition” in accounts in Japan, companies' attention to LDI would increase